

CBSE Class 12 Mathematics

Model Question Paper

(SET – 7)

Time: 3 Hours | Maximum Marks: 80

Section A (1×20 = 20 Marks) – MCQs

1. If $|A| = -1$ for a 3×3 matrix A , then $|\text{adj } A| =$
 - (a) 1
 - (b) -1
 - (c) 0
 - (d) 3
2. If $f(x) = x^4 - 4x^3 + 6x^2$, then $f''(1) =$
 - (a) 0
 - (b) 4
 - (c) 12
 - (d) -4
3. Order of differential equation

$$\left(\frac{d^3y}{dx^3}\right) + \left(\frac{d^2y}{dx^2}\right)^2 = 0$$

is

- (a) 1
 - (b) 2
 - (c) 3
 - (d) 5
4. If vectors a and b are parallel, then
 - (a) $a \cdot b = 0$
 - (b) $a \times b = 0$
 - (c) $|a| = |b|$
 - (d) $a + b = 0$
 5. $\int_0^2 x^2 dx =$
 - (a) $8/3$
 - (b) $4/3$

- (c) 2
(d) 1
6. If $P(A)=0.7$, $P(B)=0.6$ and $P(A \cap B)=0.5$, then $P(A \cup B)=$
(a) 0.8
(b) 0.6
(c) 0.7
(d) 0.5
7. $\lim_{x \rightarrow 0} \frac{\sin 5x}{x} =$
(a) 1
(b) 5
(c) 0
(d) ∞
8. If A is orthogonal matrix, then $A^{-1} =$
(a) A
(b) A^T
(c) $-A$
(d) 0
9. Distance of point $(1,2,2)$ from origin is
(a) 3
(b) $\sqrt{9}$
(c) $\sqrt{9}$
(d) 9
10. If $E(X)=3$ and $\text{Var}(X)=2$, then $E(X^2)=$
(a) 11
(b) 9
(c) 5
(d) 6
11. Derivative of $\tan^{-1} x$ is
(a) $1/(1+x^2)$
(b) $1/(1-x^2)$
(c) $\sec^2 x$
(d) x
12. $\int e^{-x} dx =$
(a) $e^{-x} + C$
(b) $-e^{-x} + C$
(c) $\ln x$
(d) $1/x$

13. If events A and B are independent, then

- (a) $P(A \cup B) = P(A) + P(B)$
- (b) $P(A \cap B) = P(A)P(B)$
- (c) $P(A \cap B) = 0$
- (d) $P(A) = P(B)$

14. If $X \sim \text{Bin}(8, 1/2)$, mean is

- (a) 8
- (b) 4
- (c) 2
- (d) $1/2$

15. Determinant of identity matrix of order 4 is

- (a) 4
- (b) 1
- (c) 0
- (d) -1

16. If A is singular matrix, then

- (a) $|A| = 1$
- (b) $|A| = 0$
- (c) $|A| = -1$
- (d) None

17. If $dy/dx = x$, then $y =$

- (a) $x^2 + C$
- (b) $x^2/2 + C$
- (c) $2x + C$
- (d) $x + C$

18. If $a = (1, 0, 0)$, $b = (0, 1, 0)$, then $|a \times b| =$

- (a) 0
- (b) 1
- (c) -1
- (d) 2

19. $\int_0^1 x^3 dx =$

- (a) $1/4$
- (b) $1/3$
- (c) 1
- (d) 0

20. Rank of zero matrix of order 4 is

- (a) 4

- (b) 1
- (c) 0
- (d) 2

Section B (2×6 = 12 Marks)

21. Find determinant of

$$\begin{bmatrix} 1 & 2 \\ 3 & 5 \end{bmatrix}$$

22. Differentiate $y = x^2 \ln x$

23. Find equation of tangent to curve $y=x^2$ at $x=1$.

24. Evaluate $\int (x^3 + 2)dx$

25. Find magnitude of vector $2i-3j+6k$.

26. A die is thrown twice. Find probability of getting doublet.

Section C (3×8 = 24 Marks)

27. Using determinants, solve:

$$x + y = 32x + 3y = 8$$

28. Find dy/dx if $x^2 + y^2 = 25$.

29. Evaluate $\int_0^1 (x + 2)dx$

30. Show that vectors $(1,2,3)$ and $(2,4,6)$ are parallel.

31. A fair coin is tossed four times. Find probability of exactly three heads.

32. Solve differential equation:

$$\frac{dy}{dx} = 4x^3$$

33. Find area bounded by curve $y=x^2$ from $x=0$ to 3.

34. Find equation of plane passing through $(1,0,0)$ and parallel to plane $x+y+z=5$.

Section D (4×6 = 24 Marks)

35. If

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 6 \\ 1 & 1 & 1 \end{bmatrix}$$

find $|A|$ and comment on invertibility.

36. Verify Rolle's Theorem for $f(x)=x^3-3x$ on $[-\sqrt{3}, \sqrt{3}]$.

37. Evaluate $\int xe^x dx$

38. Find shortest distance between lines:

$$\frac{x}{1} = \frac{y}{2} = \frac{z}{3}$$

and

$$\frac{x-1}{2} = \frac{y-1}{3} = \frac{z-1}{4}$$

39. Find mean and variance of Binomial distribution $n=6$, $p=1/3$.

40. Solve differential equation:

$$\frac{dy}{dx} + y = x$$