

CLASS X – MATHEMATICS

ANSWER KEY

(SET–3)

* SECTION – A (1 × 20 = 20 Marks)

Q1. HCF of 210 and 45 = **15** ✓ (b)

Q2. $6x - 18 = 0$

$x = 3$ ✓ (b)

Q3. $2x + y = 7$

$4x + 2y = 14$

Second is multiple of first

⇒ **Infinitely many solutions** ✓ (c)

Q4. $a = 5, d = 3$

$a_{15} = a + 14d$

$= 5 + 42$

$= 47$ ✓ (b)

Q5. Prime numbers on die = 2,3,5

Probability = $\frac{3}{6} = \frac{1}{2}$ ✓ (c)

Q6. $\cos 30^\circ = \frac{\sqrt{3}}{2}$ ✓ (b)

Q7. Distance = $\sqrt{[(5-0)^2 + (12-0)^2]}$

$= \sqrt{(25 + 144)}$

$= \sqrt{169} = 13$ ✓ (d)

Q8. $D = 4 - 4 = 0$

⇒ **Real & Equal** ✓ (b)

Q9. Area = πr^2

$= \frac{22}{7} \times 49$

$= 154 \text{ cm}^2$ ✓ (a)

Q10. Mean = $(2+4+6+8+10)/5$
= $30/5$
= **6** ✓ (c)

Q11. Area ratio = $(4/7)^2 = 16/49$ ✓ (c)

Q12. Lengths of tangents from external point are **Equal** ✓ (a)

Q13. Volume = $\pi r^2 h$
= $22/7 \times 49 \times 10$
= **1540 cm³** ✓ (a)

Q14. $\sin \theta = 0$
 $\theta = 0^\circ$ ✓ (a)

Q15. Median = **11** ✓ (b)

Q16. Mode = **2** ✓ (b)

Q17. $\sin^2 \theta + \cos^2 \theta = 1$ ✓ (b)

Q18. Surface Area = $6a^2$
= 6×36
= **216 cm²** ✓ (a)

Q19. Both true & R correct explanation ✓ (a)

Q20. Both true but R not explanation ✓ (b)

*** SECTION – B (2 × 5 = 10 Marks)**

Q21. HCF by Euclid's Division Algorithm (2 Marks)

$$657 = 306 \times 2 + 45$$

$$306 = 45 \times 6 + 36$$

$$45 = 36 \times 1 + 9$$

$$36 = 9 \times 4 + 0$$

\therefore HCF = **9**

Q22. 20th Term of AP (2 Marks)

$a = 3, d = 3$

$$\begin{aligned}a_{20} &= a + 19d \\ &= 3 + 57 \\ &= \mathbf{60}\end{aligned}$$

Q23. Solve $x^2 - 9x + 14 = 0$ (2 Marks)

$$(x - 7)(x - 2) = 0$$

$$\therefore x = 7, 2$$

Q24. Mean (2 Marks)

$$\text{Mean} = (10+20+30+40+50)/5$$

$$= 150/5$$

$$= \mathbf{30}$$

Q25. Area of Sector (2 Marks)

$$= (60/360) \times \pi \times 14^2$$

$$= 1/6 \times 616$$

$$= \mathbf{102.67 \text{ cm}^2}$$

*** SECTION – C (3 × 6 = 18 Marks)**

Q26. Solve Linear Equations (3 Marks)

$$x + 2y = 5$$

$$3x - y = 5$$

Multiply first by 1:

$$x = 5 - 2y$$

Substitute:

$$3(5 - 2y) - y = 5$$

$$15 - 6y - y = 5$$

$$15 - 7y = 5$$

$$7y = 10$$

$$y = 10/7$$

$$x = 5 - 20/7$$
$$= 15/7$$

$$\text{Solution} = (15/7, 10/7)$$

Q27. Diagonals of Parallelogram Bisect Each Other (3 Marks)

In parallelogram ABCD,
Diagonals AC and BD intersect at O.

In $\triangle AOB$ and $\triangle COD$:

$$AB = CD$$

$$\angle AOB = \angle COD \text{ (vertical angles)}$$

$$\angle ABO = \angle CDO$$

By ASA congruency,
 $AO = OC$ and $BO = OD$

Hence proved.

Q28. Median (3 Marks)

$$\text{Total } N = 30$$

$$N/2 = 15$$

$$\text{Median class} = 20-30$$

$$l = 20$$

$$f = 10$$

$$cf = 10$$

$$h = 10$$

$$\text{Median} = 20 + [(15-10)/10] \times 10$$

$$= 20 + 5$$

$$= \mathbf{25}$$

Q29. Horizontal Distance (3 Marks)

$$\tan 30^\circ = 60/x$$

$$1/\sqrt{3} = 60/x$$

$$x = 60\sqrt{3}$$

$$= \mathbf{103.92 \text{ m}}$$

Q30. Sum of 30 Terms (3 Marks)

$$a = 2, d = 3$$

$$S_{30} = 30/2 [2 \times 2 + 29 \times 3]$$

$$= 15 (4 + 87)$$

$$= 15 \times 91$$

$$= \mathbf{1365}$$

Q31. Surface Area of Sphere (3 Marks)

$$= 4\pi r^2$$

$$= 4 \times 22/7 \times 196$$

$$= \mathbf{2464 \text{ cm}^2}$$

*** SECTION – D (5 × 4 = 20 Marks)****Q32. Quadratic Formula (5 Marks)**

$$3x^2 - 5x - 2 = 0$$

$$x = [5 \pm \sqrt{(25 + 24)}] / 6$$

$$= [5 \pm 7] / 6$$

$$x = 2 \text{ or } -1/3$$

Q33. Basic Proportionality Theorem (5 Marks)

If a line parallel to one side of triangle divides other two sides proportionally,

Then $AD/DB = AE/EC$

Using similarity of triangles, theorem proved.

Q34. Probability (5 Marks)

Total balls = 15

(i) Green = $6/15 = \mathbf{2/5}$

(ii) Not red = $11/15$

Q35. Cone into Spheres (5 Marks)

$$\text{Volume cone} = 1232 \text{ cm}^3$$

$$\text{Volume sphere (r=2)}$$

$$= \frac{4}{3} \pi 8$$

$$= 33.51 \text{ cm}^3$$

$$\text{Number} = 1232 / 33.51$$

$$\approx \mathbf{37 \text{ spheres}}$$

*** SECTION – E (Case Study)****Q36. Circular Garden**

$$\text{Radius} = 35 \text{ m}$$

$$(i) \text{ Circumference} = 2\pi r$$

$$= 220 \text{ m}$$

$$(ii) \text{ Area} = 3850 \text{ m}^2$$

$$(iii) \text{ Cost} = 220 \times 80$$

$$= ₹17,600$$

Q38. Ladder Problem

$$\text{Height} = 20 \sin 30^\circ$$

$$= 10 \text{ m}$$

$$\text{Distance} = 20 \cos 30^\circ$$

$$= 17.32 \text{ m}$$

Verification:

$$1 + \tan^2 \theta = \sec^2 \theta \checkmark \text{ Verified}$$
